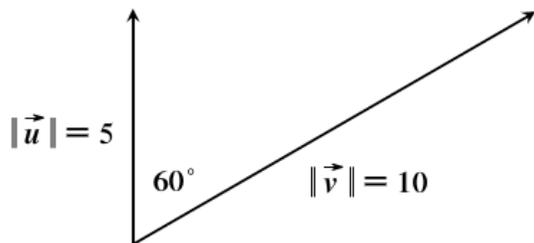


1) Find the cross product of the unit vectors.

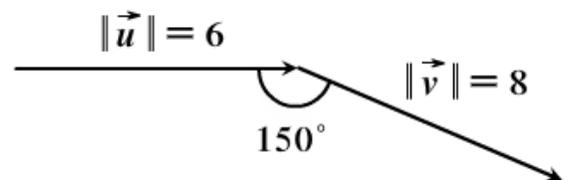
- a)  $\mathbf{j} \times \mathbf{i}$
- b)  $\mathbf{i} \times \mathbf{j}$
- c)  $\mathbf{k} \times \mathbf{i}$
- d)  $\mathbf{i} \times \mathbf{k}$

2) Find  $\|\vec{u} \times \vec{v}\|$  and determine whether  $\vec{u} \times \vec{v}$  is directed into the page or out of the page.

a)



b)



3) Given  $\vec{u} = \langle 7, 3, 2 \rangle$  and  $\vec{v} = \langle 1, -1, 5 \rangle$  find the following:

- a)  $\vec{u} \times \vec{v}$
- b)  $\vec{v} \times \vec{u}$
- c)  $\vec{v} \times \vec{v}$

4) Given the following vectors find  $\vec{w} = \vec{u} \times \vec{v}$  and show that it is orthogonal to both  $\vec{u}$  and  $\vec{v}$ .

a)  $\vec{u} = 2\mathbf{i} - 3\mathbf{j} + \mathbf{k}$ ,  $\vec{v} = \mathbf{i} - 2\mathbf{j} + \mathbf{k}$

b)  $\vec{u} = \mathbf{i} + e^t\mathbf{j} + e^{-t}\mathbf{k}$ ,  $\vec{v} = 2\mathbf{i} + e^t\mathbf{j} - e^{-t}\mathbf{k}$

c)  $\vec{u} = \langle t, t^2, t^3 \rangle$ ,  $\vec{v} = \langle 1, 2t, 3t^2 \rangle$

5) Find two unit vectors orthogonal to both  $\langle 1, -1, 1 \rangle$  and  $\langle 0, 4, 4 \rangle$ .

6) Find the area of the parallelogram that has the given vectors as adjacent sides:

a)  $\vec{u} = \mathbf{j}$ ,  $\vec{v} = \mathbf{j} + \mathbf{k}$

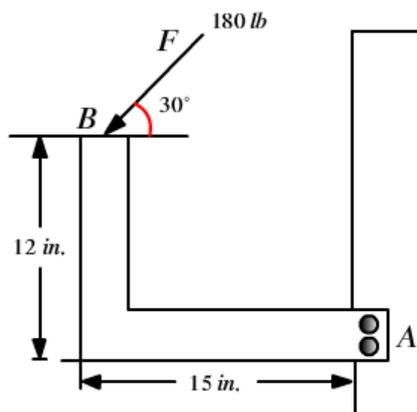
b)  $\vec{u} = \langle 3, 2, -1 \rangle$ ,  $\vec{v} = \langle 1, 2, 3 \rangle$

7) Show that  $(\vec{u} \times \vec{v}) \cdot \vec{v} = 0$  for all vectors  $\vec{u}$  and  $\vec{v}$ .

8) The vertices of a triangle are:  $(2, 1, 5)$ ,  $(-1, 3, 4)$ , and  $(3, 0, 6)$ , find the following:

- A vector orthogonal to the plane of the triangle.
- The area of the triangle.

9) A force of 180 pounds acts on the bracket shown below, determine the magnitude of the moment about A by evaluating  $\|\vec{AB} \times \vec{F}\|$ .



- 10) Find the volume of the parallelepiped with the given vertices:  $(0,0,0)$ ,  $(3,0,0)$ ,  $(0,5,1)$ ,  $(2,0,5)$ ,  $(3,5,1)$ ,  $(5,0,5)$ ,  $(2,5,6)$ ,  $(5,5,6)$ .
- 11) Use the scalar triple product to determine whether the points:  $(1,0,1)$ ,  $(2,4,6)$ ,  $(3,-1,2)$ , and  $(6,2,8)$  lie in the same plane.
- 12) A wrench 30 cm long lies along the positive  $y$ -axis and grips a bolt at the origin. A force is applied in the direction  $\langle 0,3,-4 \rangle$  at the end of the wrench. Find the magnitude of the force needed to supply 100 J of torque to the bolt.